

Comprehensive Modelling of a Capacitor Charger Boost Converter with PID Control

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I. INTRODUCTION

Electrical energy is an energy source that is widely used in everyday life. This use ranges from the household to the industrial scale. Electrical energy produced by generators must have electrical standards that are appropriate to the load; these standards include voltage, frequency, and current. When viewed from voltage standards, two types of voltage that are commonly used: direct voltage (DC) and alternating voltage

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(AC) [1]. The voltage connected to the load must have an appropriate voltage rating for the load. For DC voltage, several voltage levels are commonly used, including 6, 9, 12, 24, and 48 V. This voltage is usually obtained from a battery, accumulator, or AC voltage, which is rectified using a rectifier such as a diode [2].

The load often has different voltage specifications than the source. To obtain a varying DC voltage, a power converter is needed to produce an output voltage according to the required voltage rating. Power converters can generally be divided into two groups depending on the input voltage. If the input voltage is AC voltage, an AC-DC converter is used, which generally uses a rectifier. However, if the input voltage is a DC voltage, then a DC –DC converter is used, which has different voltage specifications from the source. To obtain a varying DC voltage, a power converter is needed that can produce an output voltage according to the required voltage rating. If the input voltage is AC voltage, an AC-DC converter is used, which generally uses a rectifier. However, if the input voltage is DC, a DC–DC converter is used [3], [4]. DC-DC converters can be divided based on the output voltage produced; these converters include buck converters, boost converters and buck-boost converters. Buck converters are used to obtain an output voltage that is lower than the input voltage, and boost converters are used to obtain an output voltage that is higher than the input voltage. Meanwhile, the buck-boost converter can increase and decrease the output voltage level so that the output voltage can be lower or higher than the input voltage [5], [6], [7]. During its development, this DC-DC converter was also used in the field of robotics. Buck converters and buck- boost converters are usually used to reduce battery voltage to supply voltage from the microcontroller [8], whereas boost converters are used to charge capacitors as an energy source in the ball-kicking system on wheeled soccer robots [9], [10], [11].

In this paper, boost converter modeling and simulation are performed to represent the charging of the capacitor used in kicking the ball on the robot. The capacitors chosen to store energy generally have high voltage and capacity specifications so that the energy used to kick the ball can be maximized. There are many approaches to modeling and simulating boost converters, including mathematical, circuit, transfer function, and state space approaches. The approach that is often used is a circuit approach that shows the converter circuit topology on a simulation platform [12]. However, circuit simulation is not fast enough compared with transfer function simulation to describe the ideal conditions of the converter. This ideal condition is useful as literature in the learning process. In addition, this paper will discuss the voltage control of the boost converter. This voltage control is necessary because the voltage from the boost converter will change when the load changes [13]. Voltage control was performed using PID control with Ziegler-Nichols 2 tuning and Routh-Hurwitz stability analysis. Modeling will be performed in MATLAB Simulink without using additional SimPowerSystems or SimElectronic blocksets.

II. RELATED WORKS

A. Boost Converter Modelling

Boost converter modeling is performed using a state-space approach. The following is the general form of the state approach written in equations 1 and 2.

$$\dot{x} = A\dot{x} + Bu \tag{1}$$

$$y = Cx + Du \tag{2}$$

The boost converter has two conditions, namely ON and OFF, which are representations of switches in the form of transistors or MOSFETs, which are used to regulate the output voltage of the boost converter. From these two conditions, an equation is obtained, which is the state of the boost converter. The boost converter circuit image is shown in Figure 2.1.



Figure 1. Boost Converter Circuit

Next, Figure 2 is presented, which shows the ON condition. This condition occurs when the MOSFET is in a closed condition because the duty cycle is HIGH and the diode is in a reverse biased condition. Therefore, the diode is in the OFF condition. The MOSFET ON condition is described as a connected cable. When in the ON state, in the i_L loop, the inductor L will experience charging from the input voltage V_S , which is denoted by U_1 . The differential equation in this situation is given by equation (3). Furthermore, the i_0 loop is 0 because there is no voltage source. The i_0 loop produces differential equation (4).



Figure 2. Boost Converter ON Condition Circuit Equivalent

$$U_1 = L \, \frac{di_L}{dt} \tag{3}$$

$$0 = C \frac{dV_C}{dt} + \frac{V_C}{R}$$
⁽⁴⁾

Equations (3) and (4) can be rearranged to form equations (5) and (6). We determine that $V_S = U_1$, x_1 is i_L and x_2 is V_C . The state space matrices A and B in equation (7) are the equations when the boost converter is in the ON state.

$$\dot{\mathbf{x}}_1 = \frac{1}{L} U_1 \tag{5}$$

$$\dot{x_2} = -\frac{x_2}{RC} \tag{6}$$

$$\begin{bmatrix} \dot{x_1} \\ \dot{x_2} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & -\frac{1}{RC} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} U_1$$
(7)

When the MOSFET is in the OFF condition, the diode is in the forward bias condition so that it is in the ON condition. The current stored in the inductor in the ON condition will decrease. However, this change in current will be resisted by the inductor by reversing the voltage polarity. Due to the voltage

reversal, the voltage from the source and from the inductor will be connected in series. This voltage will charge the capacitor through the diode, which is in the ON condition. In this condition, the capacitor stores energy from the sum of the source and inductor voltages. The equivalent circuit of the boost converter in the OFF condition is depicted in Figure 3.



Figure 3. Boost Converter OFF Condition Circuit Equivalent

By applying KVL to Figure 3, the state variables are obtained as follows.

$$V_C = u_1 - L \frac{di_L}{dt} \tag{8}$$

$$i_L = C \frac{dV_C}{dt} + \frac{V_C}{R} \tag{9}$$

Equations (8) and (9) can be rearranged to form equations (10) and (11). The state space matrices A and B in equation (12) are the equations when the boost converter is in the OFF state.

$$\dot{x_1} = -\frac{1}{L} + \frac{1}{L} U_1 \tag{10}$$

$$\dot{x_2} = \frac{1}{C} x_1 - \frac{1}{RC} x_2 \tag{11}$$

$$\begin{bmatrix} \dot{x_1} \\ \dot{x_2} \end{bmatrix} = \begin{bmatrix} 0 & -\frac{1}{L} \\ \frac{1}{C} & -\frac{1}{RC} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} U_1$$
(12)

After deriving the state space matrices A and B for the ON and OFF states of the boost converter, the average of matrices A and B needs to be found by taking into account the duty cycle d [14]. The averages of matrices A and B are shown in equations (14) and (15), respectively.

$$A = A_{ON}d + A_{OFF}(1 - d)$$

$$\overline{A} = \begin{bmatrix} 0 & 0 \\ 0 & -\frac{1}{RC} \end{bmatrix} d + \begin{bmatrix} 0 & -\frac{1}{L} \\ \frac{1}{C} & -\frac{1}{RC} \end{bmatrix} (1 - d) = \begin{bmatrix} 0 & -\frac{1 - d}{L} \\ \frac{1 - d}{C} & -\frac{1}{RC} \end{bmatrix}$$
(13)

$$\overline{B} = B_{ON}d + B_{OFF}(1-d)$$

$$\overline{B} = \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} d + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} (1-d) = \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix}$$
(14)

If equations (13) and (14) are substituted with equation (1), it will produce equation (15).

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & -\frac{(1-d)}{L} \\ \frac{(1-d)}{C} & -\frac{1}{RC} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} \frac{1}{L} \\ 0 \end{bmatrix} U_1$$
(15)

Then, to get the output state from V_C and i_L, the output state space for matrices C and D is shown in equation (16)

B. Capacitor Charging

Previous research carried out the charging process on a supercapacitor using a buck converter. The use of a buck converter is intended to regulate the voltage so that it does not exceed the voltage specifications of the 58 F 20 V

supercapacitor. The charging process was performed using a dedicated LT1074 IC. The charging process reaches the full 20 V condition within 20 s. When the supercapacitor voltage reaches full, the output current from the converter will gradually decrease [15].

III. METHODS

As can be seen in Figure 1, the boost converter has several components such as MOSFETs, inductors, capacitors, diodes, and resistors. The values of these components must be determined, so that the boost converter has the appropriate output voltage. In this paper, a boost converter is discussed to increase the voltage from 24 V to 350 V. The following is a list of component values and parameters needed for the boost converter.

Parameters	Symbol	Values
Input Voltage	V _{IN}	24 V
Output Voltage	V _{OUT}	350 V
Frequency	f	60 kHz
Input Current	I _{IN}	30 A
Voltage Ripple	δ	0.01 V
Duty cycle	d	0.9314
Inductor	L	0.0012 H
Capacitor	С	9.1242 μF
Output Currrent	I _{OUT}	2.0571 A
Resistor	R	170.14 Ω

 Table 1. 350V Boost Converter Parameters

For the initial conditions, a simulation was performed using the capacitor values according to the calculated values. This condition is performed to determine whether the boost converter has an output of 350 V. When using the capacitor in table 1, the following state-space boost converter is shown in equation (17).

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & -55.21 \\ 7515 & -644.2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 805.2 \\ 0 \end{bmatrix} U_1$$
(17)

If equation (17) is changed to a transfer function, it becomes equation (18) which is the transfer function of the boost converter output voltage.

$$V_{Cap}(s) = \frac{6051000}{s^2 + 644.2s + 415000}$$
(18)

Furthermore, the capacitor used must have a high capacity and voltage. The capacitor value was changed to $4700 \ \mu F$, which is the capacitor used in the robot. If the capacitor value is changed to this value, equation (17) can be rewritten as equation (19).

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & -55.21 \\ 14.59 & -1.251 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 805.2 \\ 0 \end{bmatrix} U_1$$
(19)

If equation (19) is changed to a transfer function, it will become equation (20) which is the transfer function for the boost converter output voltage.

$$G(s) = \frac{1.175 \cdot 10^4}{s^2 + 1.251s + 805.6} \tag{20}$$

From equation (20), the PID control parameters are calculated using the Ziegler–Nichols 2 tuning and Routh-Hurwitz stability criteria. Figure 3.1 shows a boost converter control block diagram. H(s) is a voltage divider circuit used to detect changes in the boost converter output voltage. The voltage divider circuit consists of resistors $R_1 = 150k\Omega$ and $R_2 = 11k\Omega$. When using Ziegler Nichols 2, the Kd and Ki values must be set to 0 to obtain the K_{CR} dan P_{CR} values.



Figure 4. Control Block Diagram Boost Converter

With (s) = Vs, $C(s) = V_c$, $K_i = 0$ and $K_d = 0$, the following closed-loop transfer function of the boost converter control block diagram is shown in Figure 3.1.

$$\frac{C(s)}{R(s)} = \frac{1.175 \cdot 10^4 \cdot Kp}{(s^2 + 1.251s + (805.6 + 1.175 \cdot 10^4 \cdot Kp)) \cdot H(s)}$$
(20)

To obtain the characteristics of an equation, the roots of the denominator of the transfer function equation (20) must be determined.

$$(s^{2} + 1.251s + (805.6 + 1.175 \cdot 10^{4} \cdot Kp)) \cdot H(s) = 0$$

$$s^{2} + 1.251s + (805.6 + 1.175 \cdot 10^{4} \cdot Kp) = 0$$
(21)

The Routh array from equation (21) is as follows.

$$\begin{array}{cccccccc} s^2 & 1 & 805.6 + 1.175 \cdot 10^4 \cdot Kp & 0 \\ s^1 & 1.251s & 0 & 0 \\ s^0 & 805.6 + 1.175 \cdot 10^4 \cdot Kp & 0 & 0 \end{array}$$

By reviewing Routh-Hurwitz stability in a second-order system, the values of s^0, s^1 and s^2 must be positive.

$$805.6 + 1.175 \cdot 10^{4} \cdot Kp > 0$$

$$1.175 \cdot 10^{4} \cdot Kp > -805.6$$

$$Kp > -805.6$$

$$1.175 \cdot 10^{4}$$

$$Kp > -0.068571429$$

$$(22)$$

From equation (22) the Kp value must be more than -0.068571429. In this condition, the author takes the value Kp = 1, which is used as the *Kcr* value. When Kp = 1, the characteristic equation (21) will have the following value.

$$s2 + 1.251s + 12555.6 = 0 \tag{23}$$

To determine the period of continuous oscillation, we substitute $s = j\omega$ into the characteristic equation (23).

$$(j\omega)^{2} + 1.251(j\omega) + 12555.6 = 0$$

(12555.6 - \omega^{2}) + 1.251j\omega = 0
(24)
\omega = 112.5 \nega \omega = 0

Pcr is a critical period that causes the system to oscillate periodically. We know that $\omega = \frac{2\pi}{T}$, where T is the period of the wave, which in this situation is *Pcr*. From this formula, the *Pcr* value can be determined from the ω value from equation (24).

$$\omega = \frac{2\pi}{Pcr}$$

$$Pcr = \frac{2\pi}{112.51}$$

$$Pcr = 0.0561$$

From the calculations that have been performed, the values obtained are Kcr = 1 dan Pcr = 0.0561. Next, the values of Kp, Ki and Kd can be calculated by referring to the Ziegler Nichols 2 table.

$$Kp = 0.6 \cdot Kcr$$

= 0.6 \cdot 1
= 0.6
$$Ti = 0.5 \cdot Pcr$$

= 0.5 \cdot 0.0561 (25)
= 0.02805
$$Td = 0.125 \cdot Pcr$$

= 0.125 \cdot 0.0561
= 0.0070125

With the calculations performed in equation (25), the values Kp = 0.6, Ki = 21.39 dan Kd = 0.0042075 were obtained. Next, the PID parameter values were applied to the plant boost converter.

IV. RESULTS AND DISCUSSIONS

The capacitor value will be adjusted to table 1, this aims to determine whether the boost converter can reach a voltage of 350 V, along with the output voltage response with the capacitor value according to table 1.



Figure 5. Boost Converter Output Voltage without Capacitor Change

Figure 5 shows the output voltage response of the boost converter without changing the capacitor value. The boost converter does not experience overshoot and can achieve settling time within 0.03 s. Next, the boost converter capacitor is replaced with a value of 4700 μ *F* without using feedback.



Figure 6. Boost Converter Output Voltage without Capacitor Change

After the capacitor value is changed, it can be seen in Figure 6 that the boost converter experiences underdamped oscillations with a maximum overshoot of 675 V and a settling time of 9 s. With high overshoot and a long settling time, charging the capacitor will also take longer. Therefore, PID control is used to reduce overshoot and speed up the settling time of the boost converter so that capacitor charging is

faster. The following is the voltage response of the boost converter using PID control with the Ziegler Nichols 2 tuning parameters, equation (25).



Figure 7. Boost Converter Output Voltage Response with PID Control

Figure 7 shows the boost converter response using the Ziegler–Nichols 2 tuning PID control. With PID control, the boost converter voltage experiences an undershoot at 264 V and an overshoot at 366 V. For settling time, the boost converter can stabilize at a voltage of 351 V in 1.01 s. With PID control, the settling time of the boost converter increases. However, the Boost converter still experiences undershoot below 300 V. Therefore, fine tuning was performed again on the PID control parameters.



Figure 8. Boost Converter Output Voltage Response with Fine Tuning PID Control

Figure 8 shows the boost converter voltage response with parameters Kp = 2, Ki = 90 dan Kd = 0.09. With these parameters, the boost converter has an overshoot of 388V, an undershoot of 312V and a settling time of 0.6s at a voltage of 351 V. With this fine tuning, the previous undershoot can be reduced by 48 V and the settling time is 0.4 s faster. Therefore, for the 4700 μF capacitor, PID control parameters are used from the results of fine tuning so that the charging of the capacitor is faster. Next, the PID control parameters from the fine-tuning results are tested using several large capacity capacitors.

Capacitor	Overshoot(V)	Undershoot(V)	Settling Time(s)
Value(µF)			
1500	359	307	0.464
2200	359	313	0.436
2700	360	318	0.454
3300	366	319	0.454
5600	407	302	0.802
6800	424	281	1.17
7500	438	270	1.5
8200	447	257	1.97
9100	461	239	3.53

Table 2. Boost Converter Voltage Test Results on Capacitor Changes

From the capacitor test results in table 2, as the capacitor capacity value increases, the overshoot value will increase. Meanwhile, the undershoot value of the boost converter output voltage decreases. Therefore, as the capacitor value increases, the underdamped oscillation will take longer. This is proven by the settling time value of the capacitor output voltage, which increases with the capacitor capacity value.

V. CONCLUSIONS AND RECOMMENDATIONS

PID control can reduce the overdamped oscillation time of the boost converter voltage response if there is a change in the capacitor value. With parameters Kp = 2, Ki = 90 and Kd = 0.09, a 350V boost converter with a 4700µF capacitor can achieve a settling time of 0.6s. Furthermore, along with increasing the capacitor capacity value, it is recommended to use a more adaptive controller to reduce underdamped oscillations so that the oscillations decrease, and the output voltage response can achieve steady-state faster.

VI. **REFERENCES**

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